

Monetary Factors and Inflation in Japan

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January 12, 2007

Abstract

Recently, the Bank of Japan outlined a “two perspectives” approach to the conduct of monetary policy that focuses on risks to price stability over different time horizons. Interpreting this as pertaining to different frequency bands, we use band spectrum regression to study the determination of inflation in Japan. We find that inflation is related to money growth and real output growth at low frequencies whereas the output gap is able to explain inflation at higher frequencies. Moreover, this relationship reflects causality from money growth and the output gap to inflation in the relevant frequency bands.

Keywords: spectral regression, frequency domain, Phillips curve, quantity theory.

JEL Numbers: C22, E3, E5

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1. Introduction

The role monetary aggregates should play, if any, in the conduct of monetary policy remains a controversial issue. While no major central bank relies on monetary targeting, both the European Central Bank and the Swiss National Bank attach considerable weight to monetary variables, in particular broad aggregates, in analysing and forecasting inflation. Of course, this practice reflects the fact that in both economies shocks to velocity have historically tended to be small. Indeed, research on the relationship between money growth and inflation in these economies, in the form of estimated money-demand relationships or models for forecasting inflation, typically have not found much evidence of instability over time. By contrast, in the United States, where shifts to velocity have been large and unpredictable, money plays no role in the framework of monetary policy. Indeed, the Federal Reserve recently decided to cease compiling M3 data.

In this paper we study the relationship between money growth and inflation in Japan. Doing so is interesting for several reasons. First, Japan has experienced large fluctuations in the rate of inflation in the post-1970 data we consider. Measured in terms of changes over four quarters, inflation peaked in 1974 in Japan at about 25% and reached a trough in 2002 of -1.4%. Bordo and Filardo (2005 and 2006) study the inflation experiences of a large number of countries since the late 19th century and conclude that while money growth is generally not a useful information variable for inflation in episodes in which it is low and stable, it does contain useful information in periods of high inflation and deep deflation. One would for this reason expect to find quite a strong relationship between money growth and inflation in Japan. Indeed, as we discuss below, there is a large empirical literature finding strong linkages between money and prices in Japan, although the stability of these relationships remains an unsettled issue.

Second, empirical linkages between money and prices have played an important role in the thinking about monetary policy by the Bank of Japan (BOJ). While the BOJ did announce a quarterly forecast for money growth as measured by M2 plus Certificates of Deposit (M2+CD) between 1978 and 2006, it never targeted money growth. Rather, the monetary policy framework in force since the early 1970s can arguably best be described as an eclectic monetary policy strategy characterised by an absence of an intermediate target and a

numerical ultimate target for policy.¹ This view is illustrated by a remark made by Governor Mieno in testimony to the Diet in May 1987: *“We have paid attention to the developments of the money supply, as history not only in Japan but also in other countries suggests that in the long run a higher money growth rate tends to result in a higher inflation rate. Nevertheless, the relationship between money and inflation is much more complicated than a simple causal relationship implying that a certain rate of money growth will always result in a specified hike of inflation. For this reason, it is very difficult to determine the appropriate level of monetary aggregates and we need to rely on overall judgment based on all available information at the time”* (authors’ translation). Monetary aggregates became more important when the conduct of policy changed dramatically as a consequence of the episode of quantitative easing between March 2001 and March 2006, during which the level of base money constituted the operational target for policy.²

Broadly speaking, the role of money in monetary policy has been the subject of intensive policy discussion in Japan on three occasions. The first of these was in the 1970s when it was argued (e.g., Komiya 1976) that it was not the supply shock stemming from rapid oil price increases but “excess liquidity” created by the BOJ that was responsible for the rapid inflation in 1973-1974. The next occasion was in the early 1990s when some observers asserted that the main cause of the formation and bust of the asset prices bubble in the late 1980s and early 1990s was the fact that the BOJ initially let the money supply grow excessively rapidly and subsequently reduced the growth sharply.³ The final episode started around 2000 when Japan faced deflation and short-term interest rates reached the zero lower bound. At that time some analysts advocated the adoption of monetary targeting (e.g., Meltzer 2001 and Hetzel 2004) while others were sceptical (e.g., Krugman 1998, Eggertsson and Woodford 2003 and Svensson 2003).

These conflicting views resulted in an intense policy debate about what weight the central bank should place on money in its policy strategy as well as how it should interpret the signals from movements in the monetary aggregates. Reconsidering the role of money in monetary policy in Japan is also warranted by the fact that while monetary relationships may

¹ A senior BOJ official (Suzuki 1985) referred to the BOJ’s approach as “eclectic gradualism.”

² Under the quantitative easing policy, the operational target was the Bank’s current account balance, which constitutes a major part of base money. In addition, in October 2003, the BOJ committed to a specific inflation rate by stating that it would not lift the quantitative easing policy until core CPI inflation rate turned positive.

³ See the debate between Iwata (1993) and Okina (1993).

have shifted during the recent episodes of financial instability and zero interest rates, they may now be undergoing a “normalisation” (Iwata 2006).

In analysing the relationship between money growth and inflation in Japan this study follows a number of recent papers that demonstrate that the relationship between money growth and inflation varies across frequency bands or, loosely speaking, “time horizons”.⁴ Thus, Assenmacher-Wesche and Gerlach (2006a, 2007) use spectral regression techniques to demonstrate that there is close relationship between money growth and inflation in the euro area but only at frequencies corresponding to periodicities of more than four years. Furthermore, this relationship reflects unidirectional time-series causality from money growth to inflation. Thus, money growth can heuristically be thought of as determining the “trend” of inflation. They also show that at higher frequencies, output gaps and, at the highest frequencies, import price shocks, cause inflation. Assenmacher-Wesche and Gerlach (2006b) show that similar relationships are present in Swiss data. Interestingly, these results are strikingly compatible with views of the inflation process of the European Central Bank and the Swiss National Bank, both of which continue to attach considerable importance to broad money growth as a determinant of long-run inflation while recognising that the state of the business cycle and cost-push shocks have important transitory effects on inflation.⁵

The paper is structured as follows. In the next section we provide an overview of the role played by monetary aggregates since the early 1970s in the Bank of Japan’s thinking about policy. Historically, large movements in money growth have been seen as signalling major changes in the path of aggregate demand. We also provide a brief review of the literature on the relationship between money and inflation in Japan. The key finding in that literature is that, although the recent data has not been fully examined yet, money-demand relationship are generally stable if properly specified and that money growth does contain information useful for forecasting future inflation.

In Section 3 we present our econometric model, which follows Assenmacher-Wesche and Gerlach (2006a). We assume that inflation can be decomposed into low and high-frequency components. At low frequencies, inflation is determined by the flow excess supply of money,

⁴ A time series at any point in time consists of both high and low-frequency components and thus there is no direct correspondence between frequencies and time horizons. While high-frequency fluctuations per definition cannot have long-run effects, the low-frequency components are present in the short and the long run.

⁵ This view of the inflation process has been formalised in the time domain by Gerlach (2003 and 2004), Neumann (2003), and Neumann and Greiber (2005).

defined by the growth rate of money minus the growth rate of real GDP and changes in interest rates that capture shifts in money demand. At high frequencies inflation is caused by the output gap.

In Section 4 we review the data and consider time-series plots of the relationships between money growth and inflation in Japan across frequency bands. These suggest that at low frequencies money growth leads inflation. In Section 5 we turn to the econometric results. The analysis in this section follows that of Assenmacher-Wesche and Gerlach (2006c; forthcoming) which demonstrates that this frequency-band decomposition is useful for understanding the determination of inflation also in Japan.⁶ We show that there are close linkages between inflation on the one hand, and money and output growth on the other. Furthermore, these linkages are closer at low than at high frequencies. We also show that the opportunity cost of holding broad money in Japan is better modelled by using the logarithm of interest rates, rather than interest rates themselves. Finally, we demonstrate that headline inflation can be modelled by focusing on the low frequency variation of money and output growth – the quantity theoretic variables – and the output gap.

In Section 6 we go on to show that the correlations between money growth and inflation, and the output gap and inflation, in the relevant frequency bands reflect univariate time-series causality. Finally, Section 7 offers our tentative conclusions.

2. Money and monetary policy in Japan

On 9 March 2006, the Bank of Japan lifted its quantitative easing policy and adopted a new monetary policy framework. Under the new framework, the BOJ outlined a “two perspectives” approach to the conduct of monetary policy. The first of these is an evaluation of the stance of policy in the light of expected developments in economic activity and inflation over a one-to-two-year horizon. Particular emphasis is placed on examining whether the Bank’s outlook, which is published biannually, is consistent with sustainable growth under the BOJ’s Policy Board’s understanding of price stability (currently, 0-2% CPI inflation). The second perspective is meant to address risks to sustainable growth and price stability over a longer horizon, risks that might require more flexibility in the conduct of policy than would be implied by the first perspective alone.

⁶ While they show that the same decomposition fits the US data, the low-frequency link between money growth and inflation is much less distinct in the US than in Japan and in the euro area. In the case of the UK, there appear to be no causality from money growth to inflation.

While the “two perspectives” bears some similarities with the European Central Bank’s “two pillar” approach in that both strategies would potentially allow departures from short to medium-run inflation control, the role of money is very different in the two frameworks.⁷ While the ECB specifies a reference value for the growth of M3, the BOJ does not provide an explicit role for the money stock in its conduct of monetary policy. Indeed, the background document of the new policy framework does not refer to “money” at all (BOJ, 2006).

This omission of an explicit role for money seems to reflect the fact that the BOJ no longer perceives monetary aggregates to provide useful information about future inflation. By contrast, it used to see money as an important indicator when it started to announce forecasts on money growth in the late 1970s.⁸ At the time, the BOJ appeared to think that although money might not predict small fluctuations of economic activity, a large change in the money stock would convey important signals of major shocks affecting the economy.⁹ However, more recently, the BOJ (2003) interpreted the fact that the episode of deflation coincided with modest M2+CD growth as an indication that the relationship between these variables had become unstable after the mid-1990s. As a result, it stated that

“In the current circumstances, it is difficult to obtain information about current and future economic developments or prices and furthermore about the effect of monetary policy from movements in the money stocks.” (BOJ, 2003, p. 168).

Iwata (2006) argues that the link between money, output and prices largely disappeared after 1997 as a consequence of weakness in the financial sector.

Empirical research so far is generally compatible with the BOJ’s view. First, earlier work broadly suggests that the relationship between money and economic activity has been stable and that money contains information useful for forecasting future inflation. For instance, analyses of the stability of money-demand functions tend to find that if variables representing wealth effects and/or precautionary demand are controlled for, there is little evidence for a shift in money demand (e.g., Sekine 1998 and Kimura 2001).¹⁰ In addition, research on the

⁷ Interestingly, the “two perspectives” approach was referred to by the BOJ as the “two pillar” approach in Japanese in the original documents.

⁸ Iwata (2006) and BOJ (2003) review the BOJ’s thinking about the role of money in monetary policy since the 1970s.

⁹ Examples of such shocks are the episodes of rapid inflation in the early 1970s and the formation and bust associated with the “bubble economy” in the late 1980s and early 1990s.

¹⁰ A large amount of research (mainly done in the 1990s) examines the stability of money demand in Japan with inconclusive results. For instance, Miyao (1996) and Nagayasu (2003) argue that the cointegrating

forecasting of inflation in Japan tends to find that money is indeed a useful policy indicator. For instance, Sekine (2001) shows that deviations from a long-run cointegration relationship of money demand is relevant for forecasting future inflation. Kitamura and Koike (2003) demonstrate that inflation forecasts can be improved by adding money growth as an explanatory variable.

However, consistent with the BOJ's view, more recent work points to a change in the relationship between money growth and inflation. For instance, Miyao (2005) reports that regression coefficients on money growth have become insignificant in forecasting equations for inflation and real GDP growth estimated on data from the 1993-2003 period. Kimura, Kobayashi, Muranaga and Ugai (2003) estimate a time-varying parameter vector autoregression (VAR) consisting of the output gap, the overnight call rate, inflation rate and base money growth. Comparing the impulse responses in 1985 and 2002, they observe that an increase in the monetary base had a positive effect on inflation in 1985, but not in 2002. By estimating a Markov-Switching VAR, Fujiwara (2006) also shows that the positive impact of an increase in base money on prices disappeared under the zero interest rate regime that started in February 1999.

However, these findings do not necessarily preclude the possibility that money contains information useful for understanding inflation developments. First, instead of the broad measure of money used in this paper, the latter two papers examine the effect of a change in base money under quantitative monetary easing.¹¹ Given the decline in the credit multiplier due to widespread problems in the financial sector, it might be that the relationship between narrow and broad money has become unstable but not the relationship between inflation and broad money. Second, although the relationship between money and inflation at high frequencies may have become unstable, at low frequencies the relationship might remain intact. Finally, once Japan left the quantitative easing strategy and the non-performing loan problems started to subside, the earlier money-inflation relationship may have been restored. In fact, the BOJ (2003, p. 169) foresaw that this might be the case and stated that “[in the future] it would not be unreasonable to expect large fluctuations in the money stock to once

relationship for broad money demand that could be established in older data disappeared in the late 1980s or the early 1990s. Recently, Miyao (2003), Fujiki and Watanabe (2004), Bae, Kakkar and Ogaki (2006) and Nishizaki (2006) show that at least for the demand for M1, a stable cointegrating relationship remains even after adoption of the zero interest rate regime in 1999, once the logarithm of interest rates is used to capture the opportunity cost of holding money.

¹¹ For a survey of the effect of quantitative easing monetary policy, see Ugai (2006).

again imply large fluctuations in economic activity.” Note that if disturbances to the money growth-inflation relationship are reasonably short-lived, the relationship may remain stable at low-frequencies.

3. An empirical model of inflation

In this section we present a small, reduced-form empirical model of the inflation process. The first perspective of the BOJ focuses on expected developments in economic activity over a horizon of up to two years, whereas the second perspective addresses risks to price stability in the long run. To formalize this view, we first decompose “headline” inflation, π_t , into low- (*LF*) and high-frequency (*HF*) components:

$$(1) \quad \pi_t = \pi_t^{LF} + \pi_t^{HF} .$$

Following Gerlach (2003, 2004), we hypothesise that the high-frequency movements of inflation are related to movements in the output gap, g_t .¹² As is common in the literature, we assume a time lag of one period between the variables:

$$(2) \quad \pi_t^{HF} = \alpha_g g_{t-1} + \varepsilon_t^{HF} .$$

While the BOJ is not explicit about the forces that affect inflation over the long run, we assume that the low-frequency variation of inflation can be understood in terms of the quantity theory of money, where again we lag the explanatory variables by one period:

$$(3) \quad \pi_t^{LF} = \alpha_\mu \mu_{t-1}^{LF} + \alpha_\gamma \gamma_{t-1}^{LF} + \varepsilon_t^{LF} ,$$

Here, μ_t and γ_t denote the growth rate of money and real output, and ε_t^{LF} captures shocks to low-frequency velocity. At low frequencies, the growth rate of real output is identical to the growth rate of potential. Under the quantity theory, and provided that money growth is uncorrelated with velocity shocks at low frequencies (that is, μ_t^{LF} and ε_t^{LF} are orthogonal), we expect that $\alpha_\mu = -\alpha_\gamma = 1$. Here we interpret the second perspective as an approach to understanding low-frequency movements, or variations in the “local steady-state” rate, of inflation. Similarly, we view the analysis of the real indicators (the first perspective) as an approach to predicting short-run swings in inflation around that steady state.

¹² Assenmacher-Wesche and Gerlach (2007) provide evidence that shocks to the exchange rate, to oil prices and to import prices help explain inflation at higher frequencies than the output gap in the euro area.

The main reason for why money growth is often, if not typically, regarded as an unreliable indicator of inflation is the occurrence of shifts in velocity, which tend to arise as a consequence of financial deregulation and changes in interest rates. This suggests that the information content of money growth for inflation could be enhanced by controlling for shifts in velocity arising from changes in interest rates. While this can be done at any (or all) frequency bands, here we adjust money growth in the low-frequency band, μ^{LF} , for changes in interest rates in the same frequency band, ρ^{LF} ,

$$(4) \quad \tilde{\mu}_t^{LF} = \mu_t^{LF} - \hat{\alpha}_r \rho_t^{LF}.$$

Instead of the low-frequency component of actual money growth, μ^{LF} , we use $\tilde{\mu}^{LF}$ as a regressor in the inflation equations we estimate below.¹³ The coefficient α_r is the long-run interest elasticity of money demand, which we estimate by regressing real money, $m-p$, on real output, y , and the money market interest rate, r :

$$(5) \quad m_t - p_t = \alpha_c + \alpha_y y_t + \alpha_r r_t + \varepsilon_t^m.$$

Of course, this procedure does not control for changes in velocity arising from financial innovation, so that the issue whether money growth is informative for inflation remains.¹⁴

The full model of the inflation process is thus given by:

$$(6) \quad \pi_t = \alpha_g g_{t-1} + \alpha_\mu \tilde{\mu}_{t-1}^{LF} + \alpha_\gamma \gamma_{t-1}^{LF} + \varepsilon_t,$$

where $\varepsilon_t = \varepsilon_t^{LF} + \varepsilon_t^{HF}$. Under this interpretation of the BOJ's policy strategy, it would seem appropriate to focus on "interest-rate adjusted" (or "adjusted" for short) low-frequency movements in money growth and on the output gap in analysing inflation.

4. Data

We use quarterly data from 1970 to the end of 2005. Inflation is measured as the first log difference of the CPI, money is M2+CD. Output is measured by splicing the real GDE series

¹³ Another strategy would be to include an interest rate in the inflation equation. However, the endogeneity of interest rates (which can arise because inflation impacts on long interest rates or because short-term rates are set in response to inflation) complicates estimation. Our approach only requires us to assume, as is common in the large literature on estimating money demand, that interest rates are predetermined relative to the real money stock.

¹⁴ The estimate of α_r will only be unbiased if shocks to velocity arising from financial innovations are uncorrelated with the explanatory variables in the money demand equation.

compiled by the SNA93 methodology with those by the SNA68 methodology in 1994. The interest rate is the money-market rate (call rate).

Figure 1 shows the data. Inflation declined throughout the sample period from a peak around 1973 to low and even negative rates in the 1990s. The trend in inflation over the sample period is shared by money growth. The high money growth and the subsequent rise in inflation in the early 1970s correspond to the episode of excess liquidity (see footnote 3 above). In contrast, both monetary growth and inflation remained modest after the second oil price shock in 1979. This experience led Friedman (1985) to state that “*The Bank of Japan has been the least monetarist central bank in its rhetoric, the most monetarist in its policy. It has also achieved the best results*”.¹⁵ In the late 1980s and early 1990s, while inflation remained stable (especially if we exclude the effects of the introduction of, and the increase in, the consumption tax in 1989 and 1997), the money-growth data reflect the formation and the burst of the bubble in Japanese asset markets around 1990.¹⁶ After that, both money growth and inflation remained low despite the aggressive quantitative easing after 2001.

Interest rates show marked movements in the early part of the sample but were virtually constant after 1995 when the target overnight call rate was cut to below 0.5%. The literature on money demand in Japan has shown that the opportunity cost of holding money might be better captured by the logarithm of the interest rate than by the usual semi-log specification (Miyao 2002, Fujiki and Watanabe 2004). The second row in Figure 1 therefore shows the interest rate and the log interest rate in levels (left panel) and differences (right panel).¹⁷ It is evident that considering the logarithm of the interest rate does have a sizable effect on the evolution of the opportunity cost of holding money, especially when the sample includes the recent period of low interest rates.

Next we turn to the output gap (defined as output relative to a smooth trend). To construct a measure of the trend output, we extract all variation of frequencies of more than 48 quarters from the quarterly growth rate of real output. Converting the filtered series to the time domain

¹⁵ Recently, Nelson (2006) attributes this success to the recognition by the Japanese government and the BOJ that inflation is a monetary phenomenon.

¹⁶ The combination of high money growth and stable inflation in the late 1980s puzzled the BOJ. At that time, Governor Mieno said that the rapid expansion of money stock made him feel like “*sitting on dried firewood*.” However, the BOJ kept its policy interest rate low until 1989 since there was no evidence of rising inflation.

¹⁷ To make the magnitude of log interest rate changes comparable to money growth and inflation rate, we divided the log of the interest rate in percent by 100.

and accumulating, we obtain a measure of the level of potential. The resulting output gap, which is plotted in the bottom left-hand panel of Figure 1, is very similar to the HP-filtered output gap, as indicated by the correlation coefficient of 0.95. Finally, real output growth was high in the 1970s and 80s but subsequently fell and fluctuated around zero thereafter.

As can be seen from the unit root tests presented in Table 1, all variables except for money growth are stationary. As unit root tests are known to have low power in the case of a root close to unity, we employ several tests. Whereas the Augmented Dickey Fuller (ADF) test, the Phillips-Perron (PP) test and the Elliot, Stock and Rotenberg (ERS) test the null hypothesis that the variable tested is nonstationary, the null hypothesis for the KPSS test is stationarity.¹⁸ The lag length is chosen by the Schwarz information criterion (SIC). While money growth turns out to be nonstationary, inflation is stationary according to the PP and ERS tests but nonstationary according to the ADF and the KPSS tests. Output growth, the output gap and the change in the interest rate appear to be stationary, suggesting that inflation and money growth should be integrated of the same order. One reason why these inclusive tests results may arise is the shift in money growth around 1990.¹⁹ We therefore compute the Zivot and Andrews (1992) unit-root test for money growth and inflation that allows for a break at an unknown point in the sample. Nevertheless, the test confirms that the inflation rate is stationary and that the money growth rate is nonstationary, irrespectively of whether we allow for a break in the intercept only or in the intercept and the trend. Since different orders of integration are implausible from a theoretical perspective and the tests are known to have low power against roots close to unity, we treat all variables as stationary.

To see how the empirical model in Section 3 will fit the data, we plot inflation, money growth and the output gap in different frequency bands. Figure 2 shows the relation between inflation and money growth at low and high frequencies. Following Baxter and King (1999) we define the low frequency as containing fluctuations with a periodicity of more than 32 quarters, while the high frequency contains fluctuations with periodicities between 6 and 32 quarters. At low frequencies inflation and money growth share the same trend, whereas at high frequencies the relation is negative.²⁰ Moreover, in the first part of the sample peaks in money

¹⁸ The unit root tests are discussed in Maddala and Kim (1998).

¹⁹ Nagayasu (2003) finds a break in a univariate autoregressive (AR) model of real M2+CD in 1994Q3.

²⁰ The negative correlation is smaller if money growth adjusted for interest rate changes is used. This suggests that the correlation may be due to velocity reacting to changes in policy-controlled interest rates in response to movements in inflation.

growth seem to lead peaks in inflation by 2 to 3 years, whereas peaks are less marked and occur simultaneously in the later part of the sample. Figure 3 shows the relation between the output gap and inflation at low and high frequencies. While there is a positive relation at the business-cycle frequency, the output gap does not explain the low-frequency movements in inflation.

5. Empirical methods and results

5.1 Money demand estimation

The first step in the analysis is the estimation of a money demand function to obtain the long-run interest elasticity of money demand which is needed to compute adjusted money growth. We use Dynamic Ordinary Least Squares (DOLS) as proposed by Stock and Watson (1993), include 2 leads and lags of the differenced regressors and apply an AR(4) correction to the errors.²¹ To check stability, we compute the coefficient on the interest rate recursively. Figure 4 shows that the coefficient on the interest rate decreases once the sample is extended beyond 1997. By contrast, the coefficient on the logarithm of the interest rate appears to be reasonably stable. This agrees with the results by Miyao (2002) and Fujiki and Watanabe (2004) who find that a log-log specification of money demand is stable for Japan. Moreover, Bae, Kakkar and Ogaki (2006) compare different functional forms in a non-linear cointegration framework and find that a log-log specification performs well. We therefore use the latter estimate of the long-run interest elasticity of money demand to correct low-frequency money growth for shifts in velocity induced by changes in interest rates.

5.2 Band spectrum regression

In this section we estimate band spectrum regressions, which allow the relation between a set of variables to differ between frequencies. This technique is particularly appropriate for the present case, in which we hypothesise that the output gap matters for inflation at high frequencies, while money and real output growth are correlated with inflation only at low frequencies. Corresponding to the two-perspective view of the BOJ, in the empirical work below we draw the distinction between the low and the high-frequency bands at a periodicity of 2 years. Nevertheless, in the 2-year frequency band money growth still may contain considerable noise (as suggested by the results for the euro area reported in Assenmacher-

²¹ Estimating the long-run interest elasticity by an Autoregressive Distributed Lag (ARDL) model (see Pesaran and Shin 1998) gives similar results and does also not indicate problems with instability when the logarithm of the interest rate is used.

Wesche and Gerlach (2006a)), and we therefore repeat our analysis for a split at the 4-year frequency.

Engle (1974) shows that if $y = x\beta + \varepsilon$ is a valid regression model in the time domain, it can be transformed into the frequency domain by applying a Fourier transformation to both the dependent and the independent variables. Denoting the transformed variables as \tilde{x} and \tilde{y} , the regression in the frequency domain is $\tilde{y} = \tilde{x}\beta + \tilde{\varepsilon}$. The transformation to the frequency domain does not affect the standard regression results. The estimator, $\hat{\beta}$, can be written as:

$$(7) \quad \hat{\beta} = \left[\sum_{k=0}^{T-1} \hat{f}_{xx}(\omega_k) \right]^{-1} \sum_{k=0}^{T-1} \hat{f}_{xy}(\omega_k),$$

where T is the sample size, $\hat{f}_{xx}(\omega)$ is the periodogram of the series in x at each frequency ω and $\hat{f}_{xy}(\omega)$ is a vector of cross periodograms.²² The benefit of transferring the regression model into the frequency domain is that it permits a test of the hypothesis that a specific model applies to some but not to all frequencies. In this case we premultiply the regression model by a $T \times T$ matrix A with unity on the diagonal for each included frequency and zero elsewhere,

$$(8) \quad A\tilde{y} = A\tilde{x}\beta + A\tilde{\varepsilon}, \text{ where } E(A\tilde{\varepsilon})(A\tilde{\varepsilon})^* = \sigma^2 A$$

with an asterisk, “*”, denoting the complex conjugate of the transposed matrix. Thus, to compute $\hat{\beta}$ we sum over a frequency band instead of the full range of frequencies as in equation (7).²³ If equation (7) is estimated only for a subset of frequencies, but is true for all frequencies, the estimator is consistent but inefficient as it does not use all available information. By contrast, if the model applies only to a specific frequency band, using information from all frequencies might obscure the relationship between the variables. For example, if only low-frequency shifts in money growth lead to proportional increases in inflation, confining the regression to this frequency band is likely to lead to more efficient estimates of the coefficient on money growth. Engle (1974) shows that a conventional F -test can be used to test for equality of the parameters across frequency bands.

²² Since the estimator of β averages over periodgrams, there is no need to smooth these as is necessary when estimating the spectrum.

²³ Though the cross-periodograms in equation (7) are complex, $\hat{\beta}$ will be real if the k^{th} frequency component is included along with the $T - k^{\text{th}}$ component.

The upper panel in Table 2 presents the results from band spectrum regressions for the low and high-frequency band with the distinction drawn at the 2-year frequency whereas the bottom panel shows the same regressions with a split at the 4-year frequency. The first column shows the results from a regression of the low-frequency part of inflation on low-frequency money and real output growth and the output gap. If the matrix A in equation (8) is not full rank, we have to adjust the degrees of freedom in the regression by the number of frequencies that has been filtered out. The coefficient on low-frequency output growth is minus unity whereas the point estimate for low-frequency money growth is slightly below unity. A F -test that the coefficients are unity and minus unity yields a test statistic of $F_{2,32} = 4.06$ and rejects this hypothesis at the 5% level of significance but not at the 1% level. The low-frequency part of the output gap is significant, which is not surprising since the 2-year split is above the business-cycle frequency. The second column in Table 2 shows that the results hardly change when adjusted money growth is used.

Since in the calculation of adjusted money growth the estimated interest elasticity from the first-step money-demand regression is used, this approach introduces generated regressors bias (Pagan 1984). To control for that we also present results for a system that comprises the inflation equation and the money-demand equation, imposing the cross-equation restriction on α_r . Since real M2+CD, real output and the interest rate are nonstationary, we chose an ARDL model for the money-demand equation in the system, which is valid in the case of cointegrated $I(1)$ variables and provides a convenient way to implement the cross-equation restriction on the interest elasticity, see Pesaran and Shin (1998).²⁴ To account for possible endogeneity we use lagged output and lagged changes in the low-frequency interest rate as instruments in the money-demand equation. The third column in Table 2 reports the coefficients of the inflation equation in the system. Results remain qualitatively the same though the coefficient on low-frequency output growth is somewhat higher.

The next three columns in Table 2 show the results for the high frequency band. As expected, money growth and output growth have no significant impact on high-frequency inflation, whereas the output gap has. Again, the estimates with the three different approaches are virtually identical.

²⁴ We include 4 lags of real money, one lag of output and no lag for the interest rate, which is the specification recommended by the Schwarz criterion, considering a maximum of 8 lags for each variable. Moreover, we add a dummy to account for the shift in money growth in 1990Q1. An F -test on the exclusion of the lagged levels in the error-correction form of the model confirms the existence of a long-run relationship at the 90% level of significance with a test statistic of 3.84, see Pesaran, Smith and Shin (2001).

The bottom panel of Table 2 shows the same regressions for a split at the 4-year frequency. As expected, the coefficient on money growth is closer to its theoretical value of unity as higher frequencies are excluded. A F -test of the hypothesis that the coefficients on money growth and output growth are unity and minus unity, respectively, yields a p -value of 0.23 for the regression using unadjusted money growth. By contrast, using adjusted money growth yields a p -value of 0.04 which rejects the hypothesis. However, the reason for the rejection is the large (in absolute value) the parameter on output growth, -1.62, which may reflect variables omitted from the money-demand relationship such as wealth. Since business-cycle fluctuations in this case are excluded in the low-frequency band, the output gap is insignificant. Again, the results from the joint estimation of the inflation equation and the money-demand function yield the same outcome, except that the output gap still is significant at low frequencies. At the high frequency band unadjusted money growth is significant but with the wrong sign, whereas adjusted money growth is not.²⁵ Apart from that, results are the same as before and therefore we do not discuss them.

5.3 A two-pillar Phillips curve

The band spectral regressions discussed above show that the relation between inflation, money and output growth, the interest rate change and the output gap varies by frequency. Money growth seems to be important only at low frequencies, whereas the output gap contains information about inflation at both low and high frequencies. To proceed, we follow Gerlach (2003, 2004), Neumann (2003) and Neumann and Greiber (2004) and estimate an equation for headline inflation with the output gap and the low-frequency components of money growth, output growth and the interest rate change as explanatory variables. In contrast to the regressions in the last section, the dependent variable is in this case not filtered and there is therefore no loss of degrees of freedom. To account for autocorrelation in the residuals we include four lags of the dependent variable. Our final inflation equation, which Gerlach (2003, 2004) refers to as “two-pillar Phillips curve”, is thus:

$$(8) \quad \pi_t = \beta_0 + \beta_\mu \mu_{t-1}^{LF} + \beta_\gamma \gamma_{t-1}^{LF} + \beta_g g_{t-1}^{HF} + \sum_{i=1}^4 \beta_\pi \pi_{t-i} + \varepsilon_t.$$

Table 3 presents estimates of equation (8) using the unadjusted and the adjusted money growth rate. Furthermore it also presents system estimates of equations (5) and (8). The first

²⁵ One reason for this finding is that faster money growth and higher inflation led the BOJ in the sample to raise interest rates, which in turn depressed money growth,

three columns define the low frequency band as containing fluctuations with a periodicity of more than two years whereas the last three columns use a split at the 4-year frequency. Results are broadly the same irrespectively of the estimation approach used. Except for low-frequency output growth all coefficients are significant. The coefficients on low-frequency money and output growth are roughly proportional in absolute value but with opposite signs. The last row in Table 3 gives the p -value from a test of the hypothesis that the long-run coefficients on money growth and output growth are unity and minus unity, respectively. This hypothesis is tested by a F -test for the single-equation approaches and by a likelihood-ratio test for the system estimation. In all cases the hypothesis of a unit long-run effect, as suggested by the quantity theory, cannot be rejected. Furthermore, the output gap has a positive effect on inflation as implied by standard Phillips-curve analysis.

6. Causality

While our results indicate that money growth is strongly correlated with current inflation, we have not directly tested the hypothesis that low-frequency movements in money growth cause inflation. This is important because the finding that money growth and inflation move together may simply reflect a stable money-demand function and need not imply that money growth causes inflation. To understand properly the inflation process an understanding of the patterns of causality is consequently needed.

We employ the notion of causality introduced by Granger (1969, 1980). Money growth is said to cause inflation if it contains information about future inflation that is not contained in some past values of π . The extent and direction of causality can differ between frequency bands (Geweke 1982, Granger and Lin, 1995). The fact that a stationary series is effectively the sum of uncorrelated components, each of which is associated with a single frequency ordinate, allows the full causal relationship to be decomposed by frequency.²⁶

Since the causal relation between money growth and inflation could be influenced by other variables, we follow Geweke (1984) and investigate causality across frequencies in a vector autoregression (VAR) containing inflation, money growth, the output gap and the change in

²⁶ Though the component of a series in a certain frequency band cannot be estimated without the use of a two-sided filter which destroys the chronological aspect of the causal definition, it is possible to deduce causal relationships at different frequencies without estimation of the series' components, as it is done in the band spectrum regressions.

the logarithm of the interest rate, i.e. we condition on the output gap and the change in the log interest rate when measuring causality between π_t and μ_t

The frequency-wise measure of causality suggested by Geweke (1982) and Hosoya (1991) is defined as:

$$(9) \quad M_{\mu \rightarrow \pi | Z}(\omega) = \log \left[1 + \frac{|\Psi_{12}(e^{-i\omega})|^2}{|\Psi_{11}(e^{-i\omega})|^2} \right],$$

where Ψ_{12} and Ψ_{11} are obtained from the moving average representation of a VAR that includes the variables of interest (in our case π_t and μ_t) together with the conditioning variables, Z_t ,

$$(10) \quad \begin{bmatrix} \pi_t \\ \mu_t \\ Z_t \end{bmatrix} = \begin{bmatrix} \Psi_{11}(L) & \Psi_{12}(L) & \Psi_{13}(L) \\ \Psi_{21}(L) & \Psi_{22}(L) & \Psi_{23}(L) \\ \Psi_{31}(L) & \Psi_{32}(L) & \Psi_{33}(L) \end{bmatrix} \begin{bmatrix} \eta_{1t} \\ \eta_{2t} \\ \eta_{3t} \end{bmatrix}$$

where the $\Psi_{ab}(L)$, $a, b = 1, 2, 3$ are polynomials in the lag operator, L , and η_1, η_2, η_3 are the orthogonalized shocks.²⁷

Money growth Granger-causes inflation if $\Psi_{12}(L)$ is non-zero. Breitung and Candelon (2006) show that the hypothesis $M_{\mu \rightarrow \pi}(\omega) = 0$ is equivalent to a linear restriction on the VAR coefficients and that its significance can be tested by a conventional F -test. To assess the significance of the causal relationship we compare the causality measure for $\omega \in (0, \pi)$ with the critical value of a χ^2 -distribution with 2 degrees of freedom, which is 5.99.

Figure 5 shows the causality measure over frequencies from zero to π . The Akaike criterion indicates a lag length of 5 for the VAR underlying the causality test. We find significant causality from money growth to inflation at low frequencies, and again at frequencies above 0.6π , which corresponds to 3 quarters, whereas between 13 and 3 quarters no significant causality is found.²⁸ In contrast, there is no causality from inflation to money growth at any frequency. We also test causality from the output gap to inflation and conversely. The causal

²⁷ That is, the VAR reduced-form errors are transformed into the orthogonalized errors by multiplying them with the lower triangular matrix from a Choleski decomposition of the reduced-form covariance matrix.

²⁸ Measuring frequency, ω , in fractions of π , periodicity in quarters is given by $2\pi/\omega$. Thus, a frequency of $\omega=0.1\pi$ corresponds to a periodicity of 20 quarters.

relationship from the output gap to inflation is significant except for frequencies between 10 and 5 quarters and shows a peak at the business cycle frequency of 20 quarters. We thus find that output gaps predict inflation at higher frequencies than money growth.

7. Conclusions

The empirical work presented in this paper can be summarised as follows. First and most importantly, the band spectral regressions indicate money growth is correlated – and output growth is inversely correlated – with inflation in the low frequency band, in particular when that is defined as frequencies of 4 years or more. Furthermore, that correlation reflects univariate time-series causality from money growth to inflation, implying that money growth does contain information about future inflation that is not already embedded in inflation. In the high frequency band the quantity-theoretic variables appear to be of little significance for inflation.

Second, and focussing on the case in which the distinction between high and low frequency is drawn at 4 years, the output gap is highly significant at high frequencies but not at low frequencies. Moreover, there is univariate causality from the output gap to inflation.

Third, in modelling headline inflation it seems useful to focus on the low-frequency components of money and output growth, and on the output gap. The results indicate that in the long run, an one percentage point increase in the growth rate of money at low frequencies leads to an equal increase in headline inflation. An increase in the low-frequency component of output growth depresses inflation proportionally, as suggested by monetary theory.

Fourth, the opportunity cost of holding M2+CD in Japan is better modelled by assuming that it is the logarithm of the interest rate, as opposed to the interest rate itself, that matters. The importance of this specification is clearest once data for the recent period of quantitative easing are considered.

While these results are supportive of the notion that money growth does contain information useful for predicting future inflation, since they say nothing about whether money growth is controllable, we emphasise that they do not imply that it would be desirable for the BOJ to target money growth. Nor do they imply that money growth should have any “special” status in the conduct of policy; like other macroeconomic variables, the weight attached to it in the policy process should presumably depend on how closely it is related to inflation.

Finally, we note that we have not explored whether the relationship between money growth and inflation is stable over time. The main reason for this is that since we focus on the low-frequency relationship between the variables, there is in fact little information about that relationship and it is consequently difficult to test whether it has shifted over time. Of course, this is merely the econometric equivalent of the fact that, since the relationship between money growth and inflation involves “long and variable lags”, it is difficult to know in real time whether and, if so, how the relationship has changed over time.

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Tables and Figures

Table 1. Unit root tests

Sample period: 1970Q1 to 2005Q4.

	<i>ADF</i>	<i>PP</i>	<i>ERS</i>	<i>KPSS</i>	<i>SIC lag</i>
Inflation	-2.60	-6.40*	-2.36*	1.67*	4
Money growth	-1.90	-2.03	-0.90	5.12*	1
Output growth	-3.97*	-9.29*	-3.40*	1.26*	2
Output gap	-5.21*	-3.69*	-3.66*	0.05	3
Interest rate change	-6.54*	-6.54*	-6.51*	0.06	0

Note: The last column indicates the number of lags included in the test, which were chosen by the Schwarz information criterion (SIC). The tests include a constant but no trend. The 5% critical values are -2.89 for the Augmented Dickey-Fuller (ADF) and the Phillips-Perron (PP) test, -1.95 for the Elliot, Stock and Rotenberg (ERS) test and 0.46 for the Kwiatkowski, Phillips, Schmidt and Shin (KPSS) test. An asterisk, “*”, indicates the rejection of the null hypothesis at the 5% level.

Table 2. Band spectrum regressionsEstimates of $\pi_t^i = \alpha_0 + \alpha_\mu^i \mu_{t-1}^i + \alpha_\gamma^i \gamma_{t-1}^i + \alpha_g^i g_{t-1}^i + \varepsilon_t^i$, $i = LF, HF$

Sample period: 1970Q2 to 2005Q4.

	<i>Low frequency: 2 to ∞ years</i>			<i>High frequency: 0.5 to 2 years</i>		
	Unadjusted money growth	Adjusted money growth	System estimation	Unadjusted money growth	Adjusted money growth	System estimation
Money growth	0.73** (0.13)	0.73** (0.12)	0.79** (0.07)	-0.02 (0.21)	0.07 (0.09)	0.09 (0.19)
Output growth	-0.99** (0.31)	-1.17** (0.31)	-1.32** (0.21)	0.09 (0.14)	0.08 (0.14)	0.08 (0.13)
Output gap	0.23** (0.09)	0.17* (0.08)	0.16** (0.05)	0.43* (0.21)	0.45* (0.21)	0.43* (0.19)
\bar{R}^2	0.54	0.59	0.60	0.10	0.11	0.12
Degrees of freedom	32	32		104	104	
Interest elasticity of money demand	--	-1.86* (0.84)	-2.05* (0.87)	--	-1.86* (0.84)	-1.47 (1.10)
	<i>Low frequency: 4 to ∞ years</i>			<i>High frequency: 0.5 to 4 years</i>		
	Unadjusted money growth	Adjusted money growth	System estimation	Unadjusted money growth	Adjusted money growth	System estimation
Money growth	0.85** (0.20)	0.93** (0.17)	0.88** (0.05)	-0.37* (0.15)	-0.05 (0.08)	-0.36* (0.17)
Output growth	-1.21** (0.56)	-1.62** (0.51)	-1.52** (0.20)	-0.04 (0.10)	-0.07 (0.10)	-0.05 (0.10)
Output gap	0.17 (0.12)	0.12 (0.11)	0.12** (0.04)	0.40** (0.10)	0.42** (0.10)	0.42** (0.10)
\bar{R}^2	0.61	0.71	0.76	0.17	0.13	0.07
Degrees of freedom	14	14		122	122	
Interest elasticity of money demand	--	-1.86* (0.84)	-2.03* (0.92)	--	-1.86* (0.84)	-1.42 (1.14)

Note: The dependent variable is the inflation rate at the respective frequency band. All regressions include a constant which is not shown. Newey-West (1987) corrected standard errors in parentheses; * indicates significance at the 5%, ** significance at the 1% level.

Table 3. Two-pillar Phillips curve

$$\text{Estimates of } \pi_t = \beta_0 + \beta_\mu \mu_{t-1}^{LF} + \beta_\gamma \gamma_{t-1}^{LF} + \beta_g g_{t-1}^{HF} + \sum_{i=1}^4 \beta_\pi \pi_{t-i} + \varepsilon_t$$

Sample period: 1970Q2 to 2005Q4.

	<i>Split at the 2-year frequency</i>			<i>Split at the 4-year frequency</i>		
	Unadjusted money growth	Adjusted money growth	System estimation	Unadjusted money growth	Adjusted money growth	System estimation
LF Money growth	0.18* (0.09)	0.25** (0.09)	0.22* (0.11)	0.24* (0.11)	0.33** (0.11)	0.26* (0.11)
LF Output growth	-0.09 (0.19)	-0.26 (0.21)	-0.19 (0.25)	-0.21 (0.25)	-0.46 (0.28)	-0.29 (0.28)
HF Output gap	0.68** (0.17)	0.66** (0.17)	0.66** (0.17)	0.55** (0.09)	0.54** (0.09)	0.54** (0.08)
Sum of AR coefficients	0.76** (0.08)	0.70** (0.09)	0.73** (0.10)	0.77** (0.08)	0.70** (0.09)	0.74** (0.08)
\bar{R}^2	0.61	0.62	0.64	0.67	0.68	0.69
Durbin-Watson	1.82	1.80	1.81	1.84	1.84	1.85
Interest elasticity of money demand		-1.86* (0.84)	-1.39 (1.09)		-1.86* (0.84)	-1.37 (1.10)
Test of unit long-run coefficients	0.66	0.70	0.71	0.95	0.80	0.14

Note: The dependent variable is the headline inflation rate. All regressions include a constant which is not shown. Standard errors in parentheses; * indicates significance at the 5%, ** significance at the 1% level. The last row shows the p -value from a test that the long-run coefficients of money growth and output growth are unity and minus unity, respectively. For the single-equation estimation we use a F -test, for the system estimation a likelihood ratio test.

Figure 1. Data

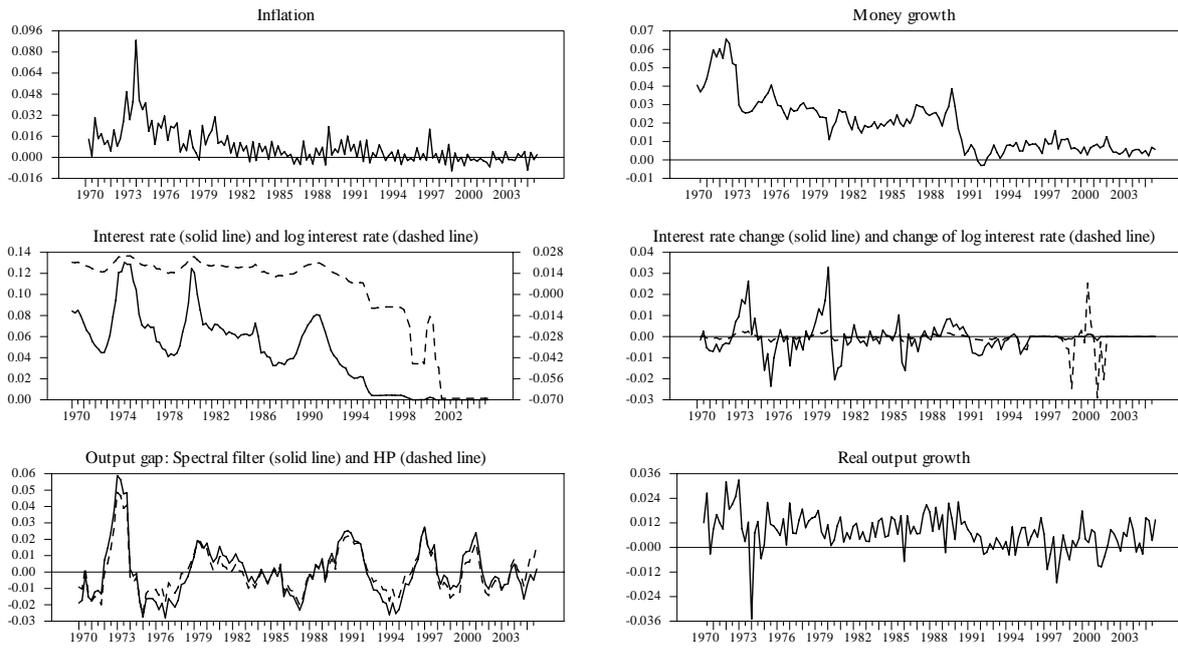


Figure 2. Inflation and money growth: low (left panel) and high frequency (right panel)

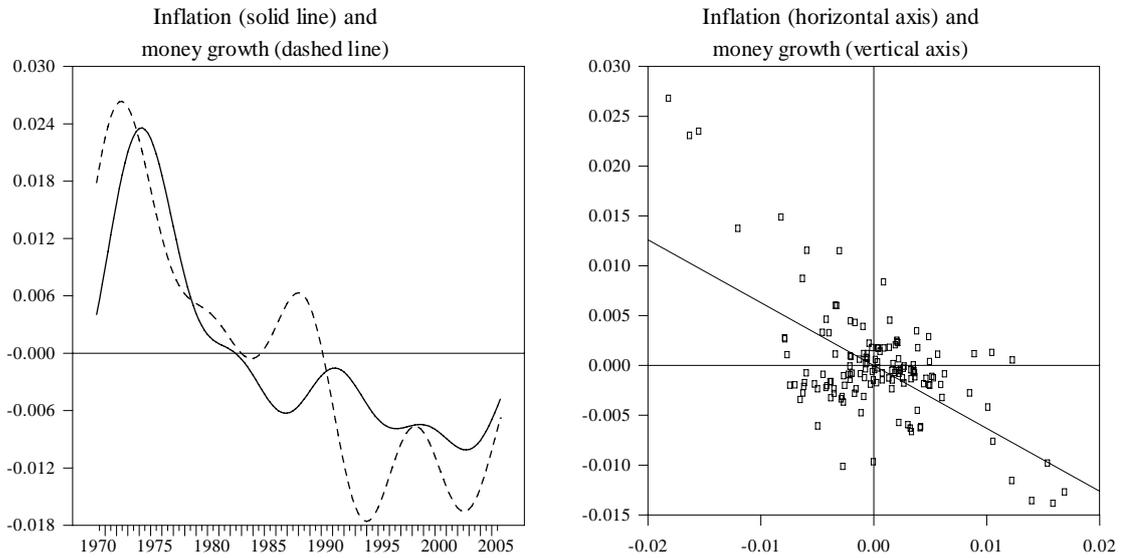


Figure 3. Inflation and output gap: low (left panel) and high frequency (right panel)

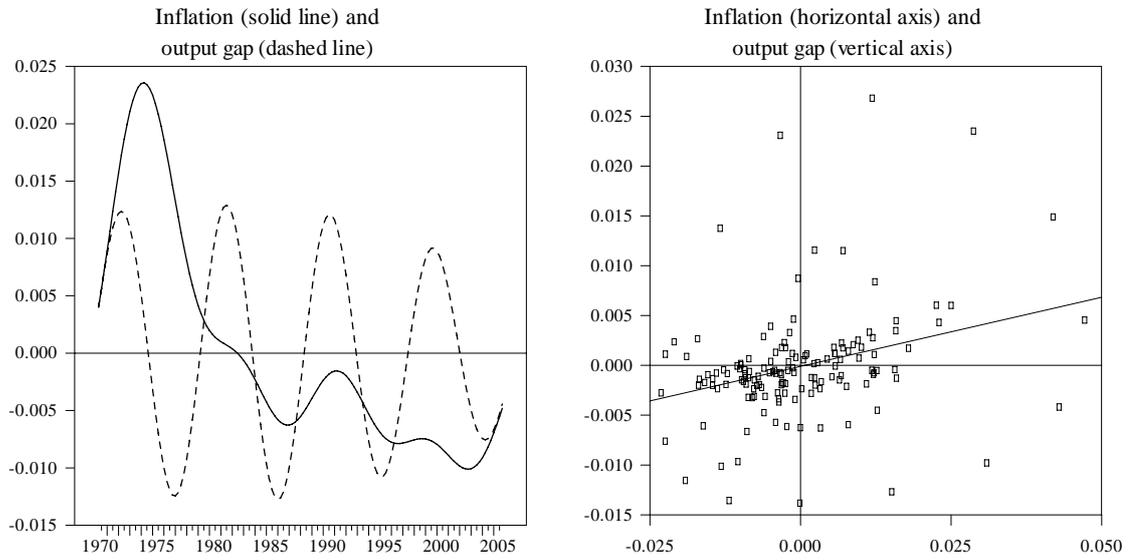
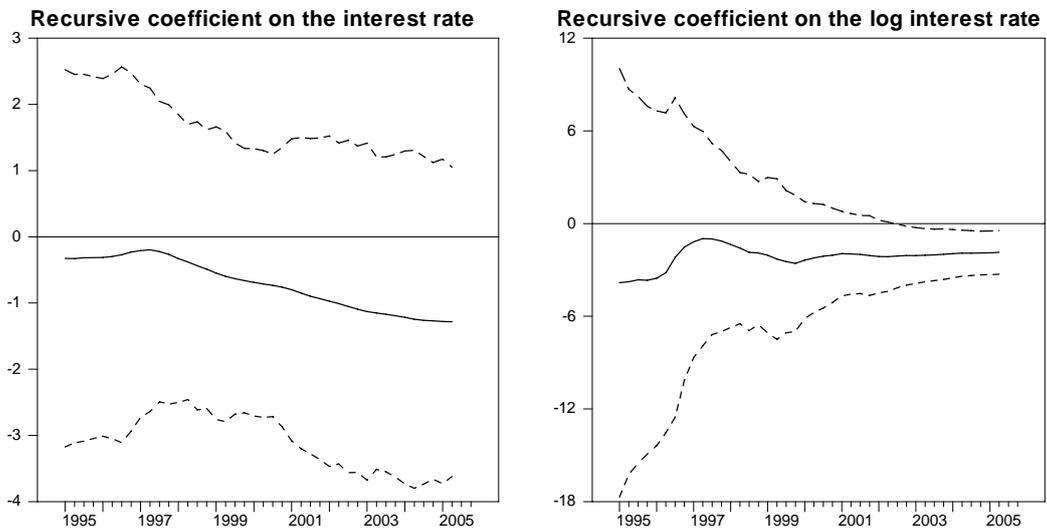
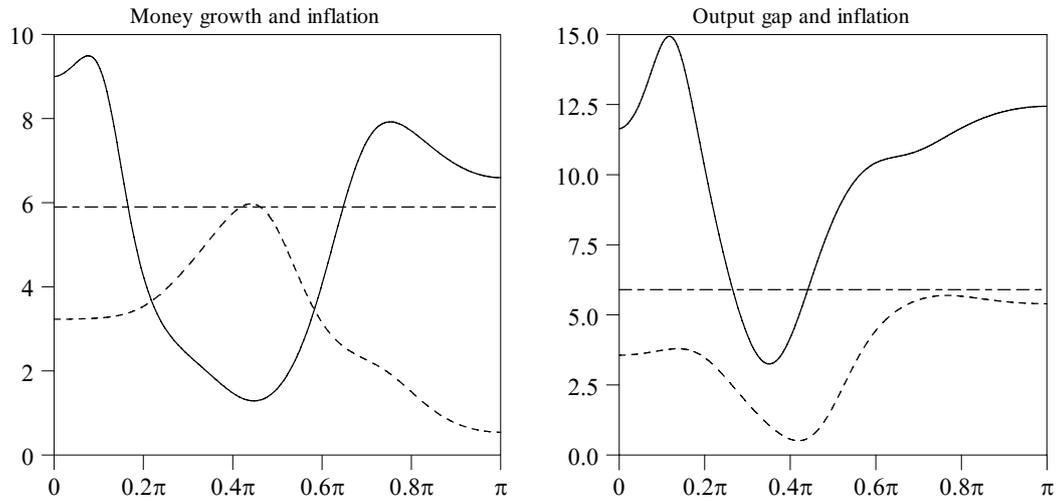


Figure 4. Interest elasticity of money demand



Note: The figure shows recursive estimates of the interest elasticity of money demand with their 95% confidence bounds, estimated by DOLS with two lags and leads of the differenced regressors and an AR(4) correction for the error term.

Figure 5. Causality



Note: The solid line shows the causality measure from money growth and the output gap to inflation, the dashed line the causality measure from inflation to the respective variable. The causality measures are derived from a VAR including inflation, money growth, the output gap and the change in the logarithm of the interest rate. The horizontal line represents the 5% critical value. The horizontal axis shows the frequency ordinates as fractions of π .